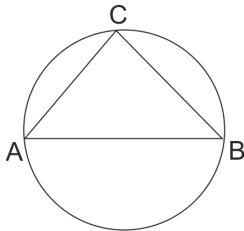


Note:-

Q.1 A) Solve Multiple choice questions.

(4)

1)



In the given figure, AB is a diameter of the circle. If $AC = BC$, then $\angle CAB$ is equal to

- a. 30° b. 60° c. 90° d. 45°

Ans. Option d.

2) The maximum number of tangents that can be drawn to a circle from a point outside it is

- a. 2 b. 1 c. one and only one d. 0

Ans. Option a.

3) A person is standing at distance of 40 m from building looking at its top at an angle of elevation 45° . Find height of church.

- a. 45m b. $\frac{40}{\sqrt{2}}$ m c. $40\sqrt{2}$ d. 40m

Ans. Option d.

4) Find the volume of cube having length of side 6.

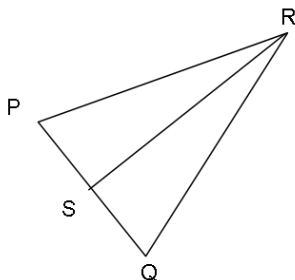
- a. 36 cm^3 b. 216 cm^3 c. 108 cm^3 d. 27 cm^3

Ans. Option b.

B) Solve the following questions.

(4)

1) In $\triangle PQR$, seg RS bisects $\angle R$. If $PR = 15$, $RQ = 20$, $PS = 12$ then find SQ.



Ans. In $\triangle PRQ$, seg RS bisects $\angle R$.

$$\frac{PR}{RQ} = \frac{PS}{SQ} \quad \dots \text{ (Angle bisector property)}$$

$$\frac{15}{20} = \frac{12}{SQ}$$

$$SQ = \frac{12 \times 20}{15}$$

$$\therefore SQ = 16$$

- 2) Radius of a circle is 10 cm. Area of a sector is 100 cm^2 . Find the area of its corresponding major sector. ($\pi = 3.14$).

Ans. Area of a major sector = Area of circle - Area of a minor sector

$$= \pi r^2 - 100$$

$$= (3.14 \times 10 \times 10 - 100)$$

$$= 314 - 100$$

$$= 214 \text{ cm}^2$$

Area of major sector = 214 cm^2

- 3) Find the slopes of the lines passing through the given points.
T(0, -3), S(0, 4)

Ans. Let T \equiv (0, -3) \equiv (x_1, y_1), S \equiv (0, 4) \equiv (x_2, y_2)

$$\text{Slope of line TS} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{4 - (-3)}{0 - 0}$$

$$= \frac{7}{0}$$

\therefore Slope of line TS = not defined

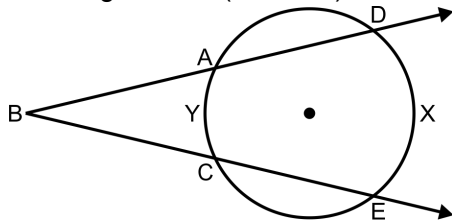
- 4) Find the length of the hypotenuse of a square whose side is 16 cm.

Ans. \square ABCD is a square.
In right angled triangle $\triangle ABC$,
 $AC^2 = AB^2 + BC^2$... (by Pythagoras theorem)
 $\therefore AC^2 = 16^2 + 16^2$
 $\therefore AC^2 = 256 + 256$
 $\therefore AC^2 = 512$
 $\therefore AC = 16\sqrt{2}$

Q.2 A) Complete the following Activities. (Any two)

(4)

- 1) In the figure, if $m(\text{arc DXE}) = 100^\circ$ and $m(\text{arc AYC}) = 40^\circ$, find $\angle DBE$.



$$\angle DBE = \frac{1}{2} [m(\text{arc DXE}) - m(\text{arc AYC})]$$

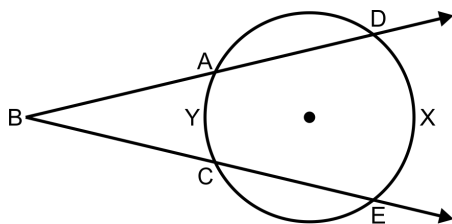
$$= \frac{1}{2} (100^\circ - 40^\circ)$$

$$= \frac{1}{2} \times 60^\circ$$

$$= 30^\circ$$

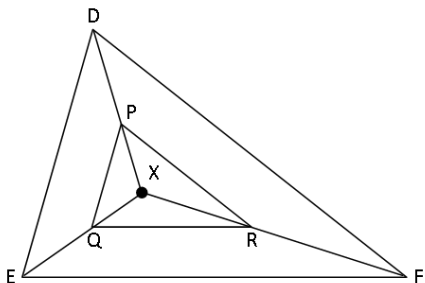
$$\angle DBE = 30^\circ$$

Ans. In the figure, if $m(\text{arc DXE}) = 100^\circ$ and $m(\text{arc AYC}) = 40^\circ$, find $\angle DBE$.



$$\begin{aligned} \angle DBE &= \frac{1}{2} [m(\text{arc } DXE) - m(\text{arc } AYC)] \\ &= \frac{1}{2} (100^\circ - 40^\circ) \\ &= \frac{1}{2} \times 60^\circ \\ &= 30^\circ \\ \angle DBE &= 30^\circ \end{aligned}$$

- 2) In the figure, X is any point in the interior of triangle. Point X is joined to vertices of triangle. Seg PQ || seg DE, seg QR || seg EF. Fill in the blanks to prove that, seg PR || seg DF.



In $\triangle XDE$, $PQ \parallel DE$... _____

$\therefore \frac{\text{XP}}{\text{PD}} = \frac{\text{XQ}}{\text{QE}}$... (I) (Basic proportionality theorem)

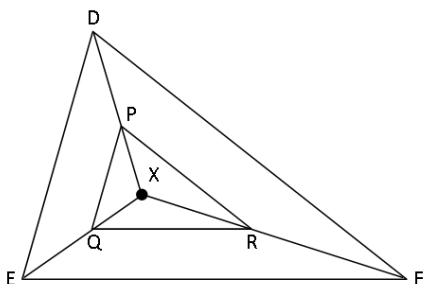
In $\triangle XEF$, $QR \parallel EF$... _____

$\therefore \frac{\text{XQ}}{\text{QE}} = \frac{\text{XR}}{\text{RF}}$... (II) (Basic proportionality theorem)

$\therefore \frac{\text{XP}}{\text{PD}} = \frac{\text{XR}}{\text{RF}}$... from (I) and (II)

$\therefore \text{seg } PR \parallel \text{seg } DF$... (Converse of basic proportionality theorem)

- Ans.** In the figure, X is any point in the interior of triangle. Point X is joined to vertices of triangle. Seg PQ || seg DE, seg QR || seg EF. Fill in the blanks to prove that, seg PR || seg DF.



In $\triangle XDE$, $PQ \parallel DE$... Given

$\therefore \frac{\text{XP}}{\text{PD}} = \frac{\text{XQ}}{\text{QE}}$... (I) (Basic proportionality theorem)

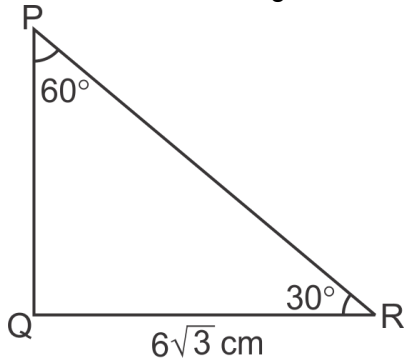
In $\triangle XEF$, $QR \parallel EF$... Given

$\therefore \frac{\text{XQ}}{\text{QE}} = \frac{\text{XR}}{\text{RF}}$... (II) (Basic proportionality theorem)

$\therefore \frac{\text{XP}}{\text{PD}} = \frac{\text{XR}}{\text{RF}}$... from (I) and (II)

$\therefore \text{seg } PR \parallel \text{seg } DF$... (Converse of basic proportionality theorem)

- 3) From the information given in the figure, find PR and PQ.



In $\triangle PQR$, $\angle Q = 90^\circ$, $\angle P = 60^\circ$, and $\angle R = 30^\circ$.

By the theorem of $30^\circ - 60^\circ - 90^\circ$ triangle,

$$QR = \frac{\sqrt{3}}{2} PR \quad \dots \text{(Side opposite to } 60^\circ)$$

$$\therefore 6\sqrt{3} = \frac{\sqrt{3}}{2} PR$$

$$\therefore PR = 6\sqrt{3} \times \frac{2}{\sqrt{3}}$$

$$\therefore PR = 12 \quad \dots (1)$$

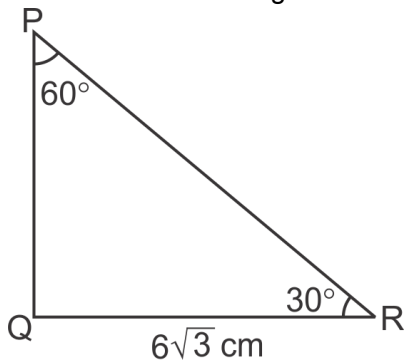
$$PQ = \frac{1}{2} PR \quad \dots (\text{ })$$

$$\therefore PQ = \frac{1}{2} \times 12 \text{ cm} \quad \dots \text{(From (1))}$$

$$\therefore PQ = 6 \text{ cm}$$

$$\mathbf{PR = 12 \text{ cm} ; PQ = 6 \text{ cm}}$$

- Ans.** From the information given in the figure, find PR and PQ.



In $\triangle PQR$, $\angle Q = 90^\circ$, $\angle P = 60^\circ$, and $\angle R = 30^\circ$.

By the theorem of $30^\circ - 60^\circ - 90^\circ$ triangle,

$$QR = \frac{\sqrt{3}}{2} PR \quad \dots \text{(Side opposite to } 60^\circ)$$

$$\therefore 6\sqrt{3} = \frac{\sqrt{3}}{2} PR$$

$$\therefore PR = 6\sqrt{3} \times \frac{2}{\sqrt{3}}$$

$$\therefore PR = 12 \text{ cm} \quad \dots (1)$$

$$PQ = \frac{1}{2} PR \quad \dots \text{(Side opposite to } 30^\circ)$$

$$\therefore PQ = \frac{1}{2} \times 12 \text{ cm} \quad \dots \text{(From (1))}$$

$$\therefore PQ = 6 \text{ cm.}$$

$$\mathbf{PR = 12 \text{ cm} ; PQ = 6 \text{ cm}}$$

- B) Solve the following questions. (Any four)**

- 1) If the area of the minor sector is 392.5 sq. cm and the corresponding central angle is 72° , find the radius ($\pi = 3.14$).

Ans. Area of minor sector = $\frac{\theta}{360} \times \pi r^2$

$$\therefore 392.5 = \frac{72}{360} \times 3.14 \times r^2$$

$$\therefore 392.5 = \frac{1}{5} \times 3.14 \times r^2$$

$$\therefore \frac{392.5 \times 5}{3.14} = r^2$$

$$\therefore 125 \times 5 = r^2$$

$$\therefore 625 = r^2$$

$$\therefore r = 25 \text{ cm} \quad \dots (\text{Taking square root on both side})$$

\therefore Radius of the circle is 25 cm.

- 2) Find the co-ordinates of point P if P is the midpoint of a line segment AB with A(- 4, 2) and B(6, 2).

Ans. (- 4, 2) = (x_1, y_1) ; (6, 2) = (x_2, y_2) and co-ordinates of P are (x, y)

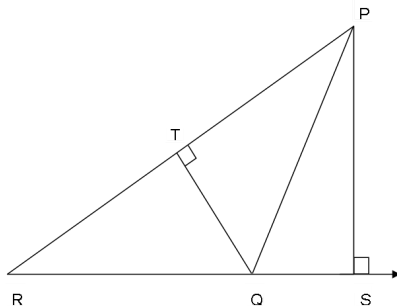
\therefore According to midpoint theorem,

$$x = \frac{x_1 + x_2}{2} = \frac{-4 + 6}{2} = \frac{2}{2} = 1$$

$$y = \frac{y_1 + y_2}{2} = \frac{2 + 2}{2} = \frac{4}{2} = 2$$

\therefore co-ordinates of midpoint P are (1, 2) .

- 3) In adjoining figure, seg PS \perp seg RQ seg QT \perp seg PR. If RQ = 6, PS = 6 and PR = 12, then find QT.



Ans. RQ = 6, PS = 6 and PR = 12 ... (Given)

Area of a triangle = $\frac{1}{2} \times \text{base} \times \text{height}$

$$A(\Delta PQR) = \frac{1}{2} \times QR \times PS$$

$$\therefore A(\Delta PQR) = \frac{1}{2} \times 6 \times 6$$

$$\therefore A(\Delta PQR) = 18 \text{ units}^2 \quad \dots (1)$$

also, $A(\Delta PQR) = \frac{1}{2} \times PR \times QT$

$$\therefore 18 = \frac{1}{2} \times 12 \times QT$$

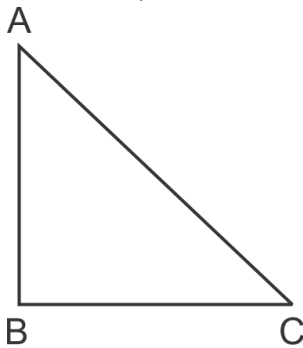
$$\therefore QT = \frac{18}{6}$$

$$\therefore QT = 3$$

QT = 3

- 4) A Ladder 10m long reaches a window 8m above the ground. Find the distance of the foot of the ladder from the base of the wall.

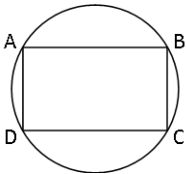
- Ans.** Seg AC represents the ladder.
 Seg BC represents the ground.
 C represents the foot of the ladder.
 B represents the base of the wall.
 A represents the window above the ground
 $AC = 10$ m, $AB = 8$ m.



- i) In $\triangle ABC$, $\angle ABC = 90^\circ$... (Base of the wall of the building \perp to the ground)
 $\therefore AB^2 + BC^2 = AC^2$... (Pythagoras theorem)
 ii) But, $AB = 8$ m, $AC = 10$ m ... (given)
 iii) $\therefore 8^2 + BC^2 = 10^2$
 $\therefore 64 + BC^2 = 100$
 $\therefore BC^2 = 100 - 64$
 $\therefore BC^2 = 36$
 $\therefore BC = \sqrt{36}$... (Taking square root)
 $\therefore BC = 6$ m

- 5) Prove that, any rectangle is a cyclic quadrilateral.

Ans.



- Let $\square ABCD$ be a given rectangle
 In $\square ABCD$,
 $\angle A = \angle B = \angle C = \angle D = \dots$ [angles of a rectangle]
 90°
 $\therefore \angle A = \angle C = 180^\circ$
 $\therefore \angle B = \angle D = 180^\circ$... [opposite angle of a quadrilateral are supplementary, then the quadrilateral is a cyclic quadrilateral]
 $\therefore \square ABCD$ is a cyclic quadrilateral

Q.3 A) Complete the following activity. (Any one)

(3)

- 1) A circus tent is cylindrical up to a height of 3.3 m and conical above it. If the radius of the base is 50 m and the slant height of the conical part is 56.4 m, find the canvas used in making the tent.

For the cylindrical part : $r = 50$ m, $h = 3.3$ m

For the conical part : $r = 50$ m, $l = 56.4$ m

Canvas used in making tent

= _____ + curved surface area of conical part

$$= \text{_____} + \pi r l \quad \dots \text{ (Formula)}$$

$$= \pi r \text{_____}$$

$$= \frac{22}{7} \times 50 \times \text{_____}$$

$$= \frac{22}{7} \times 50 (6.6 + 56.4) \quad \dots \text{ (Substituting the given values)}$$

$$= \text{_____}$$

$$= 1100 \times 9$$

$$= \text{_____}$$

The canvas used in making the tent is _____

Ans. A circus tent is cylindrical up to a height of 3.3 m and conical above it. If the radius of the base is 50 m and the slant height of the conical part is 56.4 m, find the canvas used in making the tent.

For the cylindrical part : $r = 50$ m, $h = 3.3$ m

For the conical part : $r = 50$ m, $l = 56.4$ m

Canvas used in making tent

= curved surface area of cylindrical part + curved surface area of conical part

$$= 2\pi r h + \pi r l \quad \dots \text{ (Formula)}$$

$$= \pi r (2h + l)$$

$$= \frac{22}{7} \times 50 \times (2 \times 3.3 + 56.4)$$

$$= \frac{22}{7} \times 50 (6.6 + 56.4) \quad \dots \text{ (Substituting the given values)}$$

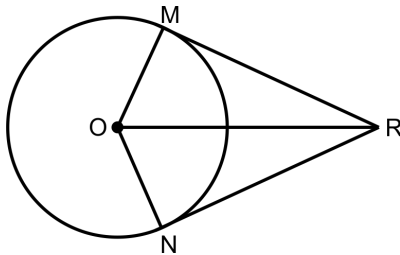
$$= \frac{1100}{7} \times 63$$

$$= 1100 \times 9$$

$$= 9900 \text{ m}^2$$

The canvas used in making the tent is 9900 m^2 .

2) Seg RM and seg RN are tangent segments of a circle with centre O. Prove that seg OR bisects $\angle MRN$ as well as $\angle MON$.



In $\triangle OMR$ and $\triangle ONR$, side $MR \cong$ side NR ... [_____]

$\angle OMR = \angle ONR = 90^\circ$... [_____]

radius $OM \cong$ _____ ... [radius of same circle]

$\therefore \triangle OMR \sim \triangle ONR$... [_____]

$\therefore \angle MRO \cong$ _____ ... [congruent angles of similar triangles]

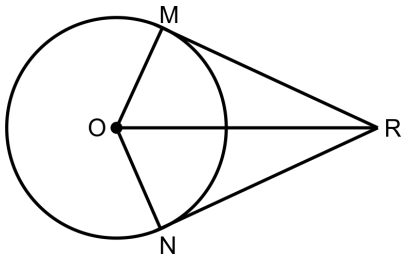
\therefore seg OR bisects $\angle MRN$

Also,

_____ $\cong \angle NOR$... [congruent angles of similar triangles]

\therefore seg OR bisects $\angle MON$ Hence proved.

Ans. Seg RM and seg RN are tangent segments of a circle with centre O. Prove that seg OR bisects $\angle MRN$ as well as $\angle MON$.



In $\triangle OMR$ and $\triangle ONR$, side
 $MR \cong$ side NR
 $\angle OMR = \angle ONR = 90^\circ$
radius $OM \cong$ radius ON
 \therefore
 $\triangle OMR \sim \triangle ONR$
 $\therefore \angle MRO \cong \angle NRO$
 \therefore seg OR bisects $\angle MRN$
Also,
 $\angle MOR \cong \angle NOR$
 \therefore seg OR bisects $\angle MON$

... [Tangents drawn from same external point to the circle are congruent]
... [Radius perpendicular to tangent]
... [radius of same circle]
... [by SAS Test of similarity]
... [congruent angles of similar triangles]
... [congruent angles of similar triangles]
Hence proved.

B) Solve the following questions. (Any two)

(6)

- 1) Ratio of areas of two triangles with equal heights is 2 : 3. If base of the smaller triangle is 6 cm then what is the corresponding base of the bigger triangle?

Ans. $\frac{A(A_1)}{A(A_2)} = \frac{2}{3}$... (given)
 $\frac{A(A_1)}{A(A_2)} = \frac{b_1}{b_2}$... {heights are same, hence area proportional to bases}

$\therefore \frac{2}{3} = \frac{b_1}{b_2}$

As $2 < 3$

$\therefore b_1 < b_2$

\therefore base of the smallest triangle = $b_1 = 6$ cm.

$\therefore \frac{2}{3} = \frac{6}{b_2}$

$\therefore b_2 \times 2 = 3 \times 6$

$\therefore b_2 = \frac{3 \times 6}{2}$

$\therefore b_2 = \frac{18}{2}$

$\therefore b_2 = 9$ cm.

\therefore Corresponding base of bigger triangle is 9 cm.

- 2) Prove the following

$\text{Cot}^2\theta - \tan^2\theta = \text{cosec}^2\theta - \sec^2\theta$

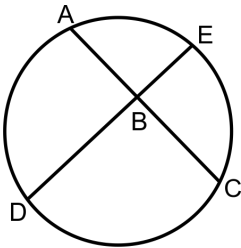
Ans. LHS = $\cot^2\theta - \tan^2\theta$

$= \left(\frac{\cos \theta}{\sin \theta}\right)^2 - \left(\frac{\sin \theta}{\cos \theta}\right)^2$... $\left[\cot\theta = \frac{\cos \theta}{\sin \theta}, \tan \theta = \frac{\sin \theta}{\cos \theta}\right]$
 $= \frac{\cos^2 \theta}{\sin^2 \theta} - \frac{\sin^2 \theta}{\cos^2 \theta}$
 $= \frac{\cos^4 \theta - \sin^4 \theta}{\sin^2 \theta \times \cos^2 \theta}$

$$\begin{aligned}
&= \frac{(\cos^2 \theta)^2 - (\sin^2 \theta)^2}{\sin^2 \theta \times \cos^2 \theta} \\
&= \frac{(\cos^2 \theta + \sin^2 \theta) \times (\cos^2 \theta - \sin^2 \theta)}{\sin^2 \theta \times \cos^2 \theta} \dots [(a + b)(a - b) = a^2 - b^2] \\
&= \frac{\cos^2 \theta - \sin^2 \theta}{\sin^2 \theta \times \cos^2 \theta} \\
&= \frac{\cos^2 \theta}{\sin^2 \theta \times \cos^2 \theta} - \frac{\sin^2 \theta}{\sin^2 \theta \times \cos^2 \theta} \\
&= \frac{1}{\sin^2 \theta} - \frac{1}{\cos^2 \theta} \\
&= \operatorname{cosec}^2 \theta - \sec^2 \theta \qquad \dots \left[\operatorname{cosec} \theta = \frac{1}{\sin \theta}, \sec \theta = \frac{1}{\cos \theta} \right]
\end{aligned}$$

∴ LHS = RHS

- 3) In chords AC and DE intersect at B. If $\angle ABE = 108^\circ$, $m(\text{arc AE}) = 95^\circ$, find $m(\text{arc DC})$.



Ans.

Given: $m(\text{arc AE}) = 95^\circ$

...
(Given)

$\angle ABE = 108^\circ$

$\angle ABE$ has its vertex inside the circle and intercepts arc AE and its vertically opposite $\angle DBC$ intercepts arc DC.

$$\angle ABE = \frac{1}{2}[m(\text{arc AE}) + m(\text{arc DC})]$$

$$\therefore 108^\circ = \frac{1}{2} \times [95^\circ + m(\text{arc DC})]$$

$$\therefore 108^\circ \times 2 = 95^\circ + m(\text{arc DC})$$

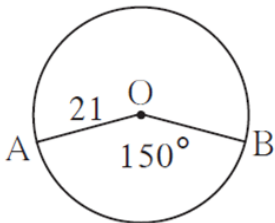
$$\therefore 216^\circ = 95^\circ + m(\text{arc DC})$$

$$\therefore m(\text{arc DC}) = 216^\circ - 95^\circ$$

$$\therefore m(\text{arc DC}) = 121^\circ$$

$$m(\text{arc DC}) = 121^\circ.$$

- 4) The measure of a central angle of a circle is 150° and radius of the circle is 21 cm. Find the length of the arc and area of the sector associated with the central angle.



Ans. $r = 21 \text{ cm}, \theta = 150, \pi = \frac{22}{7}$

$$\text{Area of the sector, } A = \frac{\theta}{360} \times \pi r^2$$

$$= \frac{150}{360} \times \frac{22}{7} \times 21 \times 21$$

$$= \frac{1155}{2} = 577.5 \text{ cm}^2$$

$$\text{Length of the arc, } l = \frac{\theta}{360} \times 2\pi r$$

$$= \frac{150}{360} \times 2 \times \frac{22}{7} \times 21$$

$$= 55 \text{ cm}$$

Q.4 Solve the following questions. (Any two)

(8)

- 1) In the following examples, can the segment joining the given points form a triangle? If triangle is formed, state the type of the triangle considering sides of the triangle. P (-2, -6), Q (-4, -2), R (-5, 0)

Ans. Let P \equiv (-2, -6) \equiv (x₁, y₁),
 Q \equiv (-4, -2) \equiv (x₂, y₂),
 R \equiv (-5, 0) \equiv (x₃, y₃),

By distance formula

$$\begin{aligned} PQ &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{[-4 - (-2)]^2 + [-2 - (-6)]^2} \\ &= \sqrt{(-4+2)^2 + (-2+6)^2} \\ &= \sqrt{(-2)^2 + (4)^2} \\ &= \sqrt{4+16} \\ &= \sqrt{20} \\ &= \sqrt{4 \times 5} \end{aligned}$$

$\therefore PQ = 2\sqrt{5}$... I

By distance formula

$$\begin{aligned} QR &= \sqrt{(x_3 - x_2)^2 + (y_3 - y_2)^2} \\ &= \sqrt{[-5 - (-4)]^2 + [0 - (-2)]^2} \\ &= \sqrt{(-5+4)^2 + (0+2)^2} \\ &= \sqrt{(-1)^2 + (2)^2} \\ &= \sqrt{1+4} \end{aligned}$$

$\therefore QR = \sqrt{5}$... II

By distance formula

$$\begin{aligned} PR &= \sqrt{(x_3 - x_1)^2 + (y_3 - y_1)^2} \\ &= \sqrt{[-5 - (-2)]^2 + [0 - (-6)]^2} \\ &= \sqrt{(-5+2)^2 + (0+6)^2} \\ &= \sqrt{(-3)^2 + (6)^2} \\ &= \sqrt{9+36} \\ &= \sqrt{45} \\ &= \sqrt{9 \times 5} \end{aligned}$$

$\therefore PR = 3\sqrt{5}$... III

PQ + QR = $2\sqrt{5} + \sqrt{5}$... [From I, II]

$$= 3\sqrt{5}$$

PR = $3\sqrt{5}$... [From III]

$\therefore PQ + QR = PR$... [From I, II, III]

∴ Points P, Q, R are collinear

∴ The line segments joining the points A, B, C do not determine a triangle.

- 2) $\triangle RHP \sim \triangle NED$, In $\triangle NED$, $NE = 7$ cm, $\angle D = 30^\circ$, $\angle N = 20^\circ$ and $\frac{HP}{ED} = \frac{4}{5}$; Construct $\triangle RHP$ and $\triangle NED$

Ans. $\triangle RHP \sim \triangle NED$... [Given]

$$\therefore \frac{RH}{NE} = \frac{HP}{ED} = \frac{RP}{ND} = \frac{4}{5}; NE = 7 \dots [\text{c.s.s.t}]$$

$$\therefore \frac{RH}{NE} = \frac{4}{5}$$

$$\therefore \frac{RH}{7} = \frac{4}{5}$$

$$\therefore RH = \frac{4 \times 7}{5} = \frac{28}{5}$$

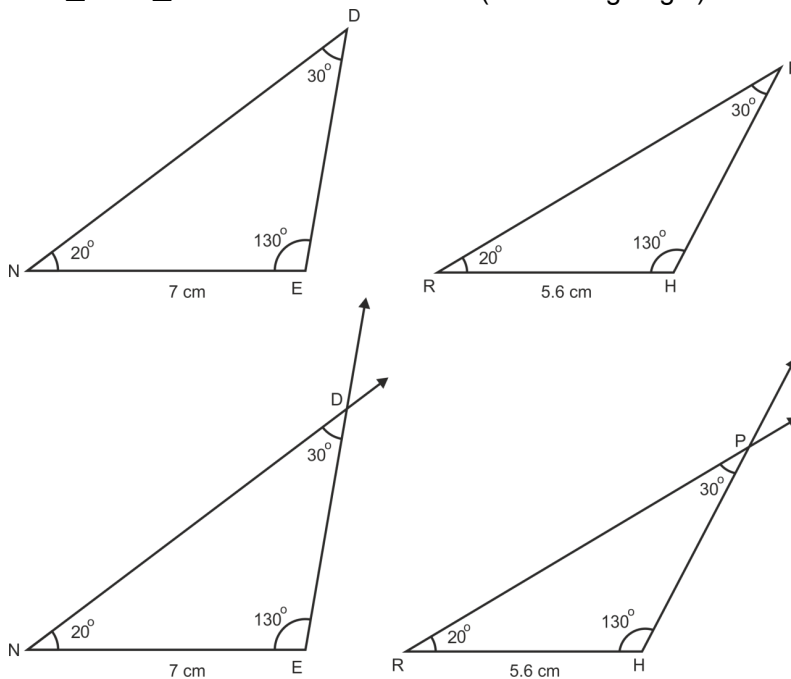
$$\therefore RH = 5.6$$

$$\angle R = \angle N = 20^\circ$$

$$\angle P = \angle D = 30^\circ$$

$$\therefore \angle H = \angle E = 130^\circ$$

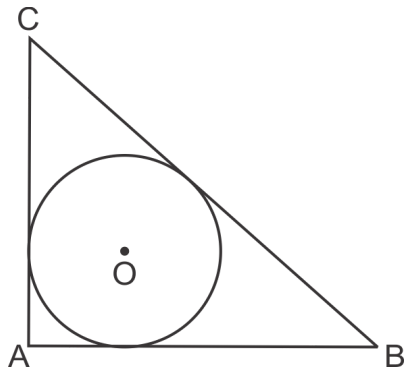
... (Remaining angle)



$\triangle RHP$ and $\triangle NED$ are the required triangles

- 3) $\triangle ABC$ is a right angled triangle with $\angle A = 90^\circ$. A circle is inscribed in it. The lengths of the sides containing the right angle are 6 cm and 8 cm.

Find the radius of the circle.



Ans. In $\triangle CAB$,
 $m\angle CAB = 90^\circ$... (Given)

\therefore By Pythagoras theorem,

$$BC^2 = AC^2 + AB^2$$

$$BC^2 = (6)^2 + (8)^2$$

$$BC^2 = 36 + 64$$

$$BC^2 = 100$$

$$BC = \sqrt{100}$$

$$= 10 \text{ cm}$$

Let the radius of the circle
be r cm.

\therefore $OP = OQ = r$... (Radii of the same circle)

$$m\angle OPA = 90^\circ$$

$$m\angle OQA = 90^\circ$$
 ... (ii) [Tangent is perpendicular to the radius]

\therefore In $\square APOQ$,

$$m\angle PAQ = 90^\circ$$
 ... (Given)

$$m\angle OPA = 90^\circ$$
 ... [From (ii)]

\therefore $\square APOQ$ is a rectangle ... [Definition of a rectangle]

$$OQ = AP = r$$

\therefore $OP = AQ = r$... [Opp. sides of a rectangle are congruent]

$$AC = AP + CP$$
 ... [A - P - C]

$$6 = r + CP$$

\therefore $CP = (6 - r)$ cm

$$AB = AQ + BQ$$
 ... [A - Q - B]

$$8 = r + BQ \quad BQ = (8 - r) \text{ cm}$$

\therefore $CP = CR = 6 - r$ cm ... [The length of two tangent segments to the circle drawn from an external point are equal]

$$BQ = BR = 8 - r \text{ cm}$$

\therefore $BC = BR + CR$... [B - R - C]

$$10 = 8 - r + 6 - r$$

$$10 = 14 - 2r \quad 2r = 14 - 10$$

$$2r = 4 \quad r = 2 \text{ cm}$$

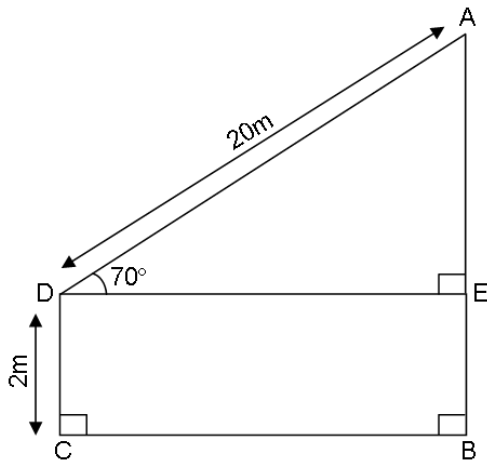
\therefore Radius of the circle is 2 cm

Q.5 Solve the following questions. (Any one)

(3)

- 1) A ladder on the platform of a fire brigade van can be elevated at an angle of 70° to the maximum. The length of the ladder can be extended upto 20m. If the platform is 2m above the ground, find the maximum height from the ground upto which the ladder can reach. ($\sin 70^\circ \approx 0.94$)

Ans.



Here, AD represents the ladder.

$$\therefore AD = 20\text{m}$$

At point D, angle of elevation is 70° .

$$\therefore m\angle EDA = 70^\circ$$

The lower end of the ladder fitted on fire truck is 2m above the ground.

$$\therefore DC = 2\text{m}$$

Now $\square BCDE$ is a rectangle.

$$\therefore DC = EB = 2\text{m}$$

In $\triangle AED$, $m\angle AED = 90^\circ$

$$\sin 70^\circ = \frac{AE}{AD}$$

$$\therefore 0.94 = \frac{AE}{20}$$

$$\therefore AE = 20 \times 0.94$$

$$\therefore AE = 18.8\text{m}$$

$$AB = AE + EB$$

$$\therefore AB = 18.8 + 2$$

$$\therefore AB = 20.8\text{m}$$

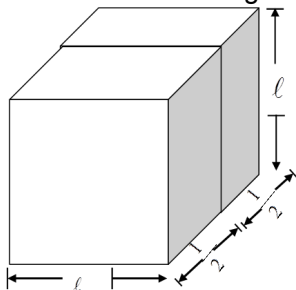
The maximum length of other end of the ladder is 20.8m away from the ground.

... [Each angle is 90°]

... [Opposite sides of rectangle are congruent]

... [A-E-B]

- 2) A solid cube is cut into two cuboids exactly at middle as shown in figure. Find the ratio of the total surface area of the given cube and that of the cuboid.



- Ans.** For the solid cube, length of edge = l
 Total surface area of cube = $6l^2$ sq. units ... (i)
 For the cuboid
 length = length of cube = l
 height = length of cube = l

$$\text{breadth} = \frac{\text{length of cube}}{2} = \frac{l}{2}$$

$$\text{Total surface area of each cuboid} = 2 (lb + bh + hl)$$

$$= 2 \left[l \times \frac{l}{2} + \frac{l}{2} \times l + l \times l \right]$$

$$= 2 \left[\frac{l^2}{2} + \frac{l^2}{2} + l^2 \right]$$

$$= 2 \left[\frac{2l^2}{2} + l^2 \right] = 2[l^2 + l^2] = 4l^2 \quad \dots(\text{ii})$$

$$\text{Total surface area of each cuboid} = 4l^2 \text{ sq. units.}$$

$$\therefore \frac{\text{Total surface area of cube}}{\text{Total surface area of cuboid}} = \frac{6l^2}{4l^2} \quad \dots[\text{From (i) and (ii)}]$$

$$= \frac{3}{2}$$

\therefore The ratio of total surface area of the given cube and that of cuboid is 3 : 2